



University  
of Victoria

Graduate Studies

Notice of the Final Oral Examination  
for the Degree of Doctor of Philosophy

of

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MSc (Georg-August-Universität Göttingen, 2014)  
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**“Poincaré self-duality of  $A\theta$ ”**

Department of Mathematics and Statistics

Tuesday, March 17, 2020

8:30 A.M.

Clearihue Building

Room B007

Supervisory Committee:

Dr. Marcelo Laca, Department of Mathematics and Statistics, University of Victoria (Co-Supervisor)

Dr. Heath Emerson, Department of Mathematics and Statistics, UVic (Co-Supervisor)

Dr. Ian Putnam, Department of Mathematics and Statistics (Member)

Dr. Julio Navarro, Department of Physics and Astronomy, UVic (Outside Member)

External Examiner:

Dr. Bram Mesland, Mathematisch Instituut, Leiden University

Chair of Oral Examination:

Dr. Daniel Bub, Department of Psychology, UVic

## Abstract

The irrational rotation algebra  $A_\theta$  is known to be Poincaré self-dual in the KK-theoretic sense. The spectral triple representing the required K-homology fundamental class was constructed by Connes out of the Dolbeault operator on the 2-torus, but so far, there has not been an explicit description of the dual element. We will geometrically construct, for any non-trivial element  $g$  of the unimodular group, a finitely generated projective module  $L_g$  over  $A_\theta \otimes A_\theta$  out of a pair of transverse Kronecker flows on the 2-torus. For upper triangular  $g$ , we will find an unbounded cycle representing the dual of said module under Kasparov product with Connes' class, and prove that this cycle is invertible in  $\text{KK}(A_\theta, A_\theta)$ , allowing us to 'untwist'  $L_g$  to an unbounded cycle representing the unit for the self-duality of  $A_\theta$ .