



University  
of Victoria

Graduate Studies

Notice of the Final Oral Examination  
for the Degree of Master of Science

of

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BSc (University of Waterloo)

**“A Study on HL-LHC Beam-Beam Resonances Using a Lie  
Algebraic Weak-Strong Model”**

Department of Physics and Astronomy

Friday, October 11, 2019

1:00 P.M.

Clearihue Building

Room B007

Supervisory Committee:

Dr. Shane Koscielniak, Department of Physics and Astronomy, University of Victoria (Co-Supervisor)

Dr. Dean Karlen, Department of Physics and Astronomy, UVic (Co-Supervisor)

External Examiner:

Dr. Alex Dragt, Department of Physics, University of Maryland

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Dr. Monica Prendergast, Department of Curriculum and Instruction, UVic

## **Abstract**

This thesis studies the resonances driven by beam-beam interactions of the planned High Luminosity upgrade to the Large Hadron Collider (HL-LHC) using a Lie algebraic formalism. With the suggested lattice for the HL-LHC, using the accelerator code MadX, bunch data for 70 bunches over the two interaction regions (IRs), ATLAS and CMS, was computed. This data was used to create a 70 impulse beam-beam Weak-Strong model combining both long-range and head-on interactions. An effective Hamiltonian was derived for the system. Along with a width formula, these are used to analyze the system in frequency space. As algebraically derived in this thesis, resonances of order  $q$  can be removed by phase-shifting the both vertical and horizontal phase advances between interaction points by  $\frac{\pi}{q}$ . Namely, the 16th order resonances close to the proposed working point of (62.31,60.32) can be weakened by phase advances close to  $\frac{\pi}{16}$ . This is reflected in frequency space plots of the effective Hamiltonian and of the width formula. Resonances are significantly weakened if phase advances are within  $10^{-3}$  of the ideal ones; the phasing needs not be exact. The effect of crossing angle was briefly investigated; according to the effective Hamiltonian and width formula, beam-beam resonances cannot be significantly improved by increasing the tentative crossing angle of  $590 \mu rad$ , yet decreasing the angle significantly strengthens the resonances of the system. A new working point (0.475,0.485) suggested from a previous study was investigated; it lies away from dangerous resonances according to the tools used in this thesis, and should be investigated further.